

Calcoliamo

$$\int_{-1}^2 7x^2(x^3 + 1)^{-\frac{1}{2}} dx.$$

Osserviamo che la derivata del radicando  $x^3 + 1$  vale  $3x^2$ ) e dunque

$$\begin{aligned}\int_{-1}^2 7x^2(x^3 + 1)^{-\frac{1}{2}} dx &= \int_{-1}^2 \frac{7x^2}{\sqrt{x^3 + 1}} dx = \frac{7}{3} \int_{-1}^2 \frac{3x^2}{\sqrt{x^3 + 1}} dx = \\ &= \frac{7}{3} \left[ 2\sqrt{x^3 + 1} \right]_{-1}^2 = \frac{7}{3} \cdot 6 = 14.\end{aligned}$$